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Quantifying the role of thermal motion in free-space light-atom interaction

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We demonstrate 17.7(1)% extinction of a weak coherent field by a single atom. We observe a shift of the resonance frequency and a decrease in interaction strength with the external field when the atom, initially at 21(1) μK, is heated by the recoil of the scattered photons. Comparing to a simple model, we conclude that the initial temperature reduces the interaction strength by less than 10%.

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I. INTRODUCTION

The prospects of distributed quantum networks have triggered much effort in developing interfaces between single photons and single atoms (or other quantum emitters) [1]. A major challenge lies in increasing the interaction strength of the atom with incoming photons, which is a key ingredient for efficient transfer of quantum information from photons to atoms. While cavity-QED experiments have made tremendous progress in this direction [2,3], it remains an open question whether (near-)deterministic absorption of single photons is also possible without a cavity [4–7].

Single trapped atoms are a particularly good experimental platform for quantitative comparisons of light-matter experiments with quantum optics theory. The clean energy level structure and the trapping in ultrahigh vacuum permits deriving the interaction strength with a minimum of assumptions. In a free-space light-atom interface (as opposed to a situation with light fields in cavities with a discrete mode spectrum), the interaction strength is characterized by a single parameter, the spatial mode overlap $\Lambda \in [0,1]$, which quantifies the similarity of the incident light field to the atomic dipole mode [8,9]. The development of focusing schemes with large spatial mode overlap is a longstanding theoretical [10–14] and experimental [4,15–23] challenge. Approaches with multielement objectives [4,16,17,23], singlet [18,24] and Fresnel lenses [25], and parabolic mirrors [26,27] have been used with various single-emitter systems. However, the interaction strengths observed with these configurations [13,22] have fallen short of their theoretically expected capabilities. Consequently, a better understanding of the underlying reasons is necessary to further improve the interaction strength. Aside from imperfections of the focusing devices, the finite positional spread of the single atomic emitter is commonly suspected to reduce the interaction [28].

In this paper, we present a light-atom interface based on a high numerical aperture lens and quantify the effect of insufficient localization of the atom on the light-atom interaction. Initially at sub-Doppler temperatures, we heat the atom in a well-controlled manner by scattering near-resonant photons and obtain a temperature dependency of the interaction strength and resonance frequency.

This paper is organized as follows. In Sec. II, we describe the optical setup and the measurement sequence. We then characterize the light-atom interaction strength by a transmission (Sec. III) and a reflection (Sec. IV) measurement and present the dependence of the light-atom interaction on the positional spread of the atom in Sec. V.

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II. EXPERIMENTAL SETUP AND MEASUREMENT SEQUENCE

The core of the optical setup is a pair of high numerical aperture lenses L_1 and L_2 (NA = 0.75, focal length $f = 5.95$ mm; see Fig. 1). A single ^{87}Rb atom is trapped at the joint focus of these lenses with a far-off-resonant, red-detuned optical dipole trap (852 nm) [29,30]. The circularly polarized (σ^+) trap has a depth of $U_0 = k_B \times 2.22(1)$ mK, with measured radial frequencies $\omega_x/2\pi = 107(1)$ kHz and $\omega_y/2\pi = 124(1)$ kHz, and an axial frequency $\omega_z/2\pi = 13.8(1)$ kHz.

We probe the light-atom interaction by driving the closed transition $5S_{1/2}, F{=}2, m_F = -2$ to $5P_{3/2}, F{=}3, m_F = -3$ near 780 nm. The spatial mode of the incident probe field is defined by the aperture of the single-mode fiber, the collimation lens C_1, and the focusing lens L_1. The beam profile before L_1 is approximately Gaussian, with a waist $w_L = 2.7$ mm. Following [13,31], the spatial mode overlap Λ of the circularly polarized Gaussian mode focused by an ideal lens with the dipole mode of a stationary atom depends on the focusing strength $u := w_L/f$,

$$\Lambda = \frac{3}{16u^3} e^{2/u^2} \left[\Gamma\left(-\frac{1}{4}, \frac{1}{u^2}\right) + u\Gamma\left(\frac{1}{4}, \frac{1}{u^2}\right)\right]^2, \quad (1)$$

where $\Gamma(a,b)$ is the incomplete gamma function. For our experimental parameters, we expect $\Lambda = 11.2\%$.

The experimental sequence used in Secs. III–V is depicted in Fig. 2. After loading a single atom into the dipole trap, the atom is cooled by polarization gradient cooling (PGC) [32]. For efficient cooling, we apply an additional σ^--polarized dipole field (852 nm) injected through the same optical fiber as the σ^+-polarized dipole field. The σ^--polarized dipole field, which is switched off after the PGC interval, originates from an independent laser running several hundreds of GHz detuned from the σ^+-polarized dipole field. Subsequently, a bias magnetic field of 0.74 mT is applied along the optical axis, and the atom is prepared in the $5S_{1/2}$, $F{=}2$, $m_F = -2$ state by optical pumping. Next, the probe field is switched on for a duration t_p during which the detection events at avalanche photodetectors (APD) D_b and D_f are recorded. Finally, we perform a reference measurement to determine the power of

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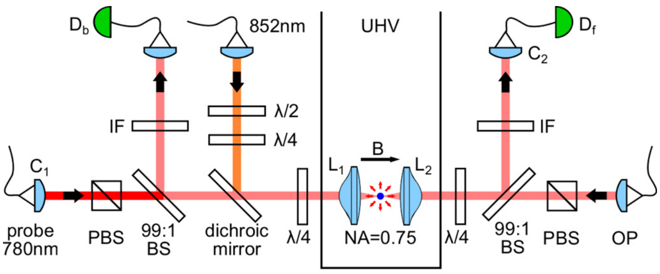

FIG. 1. Setup for probing light-atom interaction in free space. D: detector; UHV: ultrahigh vacuum chamber; IF: interference filter centered at 780 nm; $\lambda/2$: half-wave plate; $\lambda/4$: quarter-wave plate; C: fiber coupling lens; PBS: polarizing beam splitter; BS: beam splitter; L: high numerical aperture lens; B: magnetic field; OP: optical pumping.

the probe pulse. Optically pumping to the $5S_{1/2}, F{=}1$ hyperfine state shifts the atom out of resonance with the probe field by 6.8 GHz. The probe pulse is reapplied for a time t_p, and we infer the average number of incident probe photons at the position of the atom from counts at detector D_f during the reference pulse, taking into account the optical losses from the position of the atom to detector D_f.

We determine the detection efficiencies of D_b and D_f by comparing against a calibrated pin photodiode and a calibrated APD to $\eta_\mathrm{b} = 59(3)\,\%$ and $\eta_\mathrm{f} = 56(4)\,\%$, respectively. The experimental detection rates presented in the following are background corrected for 300 cps at detector D_b and 155 cps at detector D_f.

III. EXTINCTION MEASUREMENT

In this section, we describe an extinction measurement to determine the spatial mode overlap Λ between probe and atomic dipole mode. For this, we compare the transmitted power through the system during the probe and the reference interval. To detect the transmitted power, the probe mode is recollimated by the second aspheric lens L_2 and then coupled into a single-mode fiber directing the light to the forward detector D_f. The total electric field $\vec{E}'(\vec{r})$ of the light moving away from the atom is a superposition of the probe field $\vec{E}_\mathrm{p}(\vec{r})$ and the field scattered by the atom $\vec{E}_\mathrm{sc}(\vec{r})$:

$$\vec{E}'(\vec{r}) = \vec{E}_\mathrm{p}(\vec{r}) + \vec{E}_\mathrm{sc}(\vec{r}). \tag{2}$$

The electric field amplitude $E_\mathrm{f} = \int \vec{E}'(\vec{r})G^*(\vec{r})dS$ at the detector D_f is given by the spatial mode overlap of the total

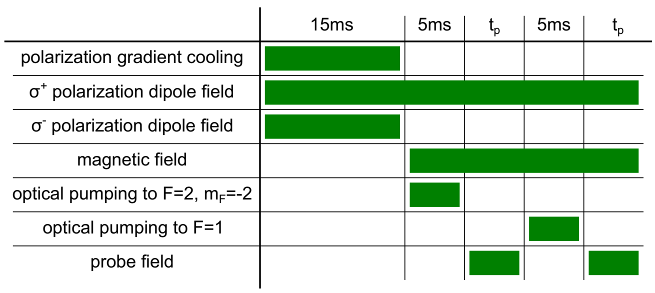

FIG. 2. Experimental sequence to probe the light-atom interaction.

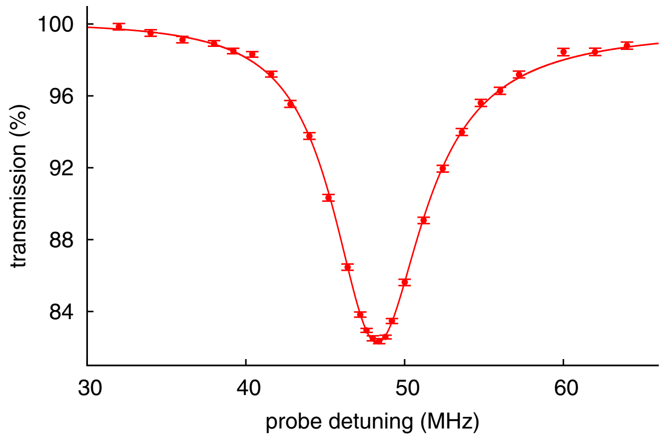

FIG. 3. Transmission measurement of a weak coherent probe beam. The solid line is a fit of Eq. (3) with free parameters: linewidth $\Gamma/2\pi = 6.9(1)$ MHz, frequency shift $\delta\omega = 48.03(3)$ MHz, spatial overlap $\Lambda = 4.67(2)\,\%$, and phase $\phi_0 = 0.13(1)$ rad ($\chi^2_\mathrm{red} = 1.01$), resulting in a resonant extinction of $\epsilon = 17.7(1)\%$. Error bars represent one standard deviation due to propagated Poissonian counting uncertainties.

electric field with the collection mode $G(\vec{r})$ (dS is a differential area element perpendicular to the optical axis) [20]. In this configuration, Λ cannot be deduced from the transmitted power without knowledge or assumptions about this mode overlap [15–19,33]. The relative transmission $\tau(\omega_\mathrm{p})$, which is the optical power at detector D_f normalized to the reference power, contains Lorentzian and dispersionlike terms [17],

$$\begin{aligned}\tau(\omega_\mathrm{p}) =& 1 + A^2\mathcal{L}(\omega_\mathrm{p}) + 2A\mathcal{L}(\omega_\mathrm{p})\\ &\times \left[(\omega_\mathrm{p} - \omega_0 - \delta\omega)\sin\phi - \frac{\Gamma}{2}\cos\phi\right],\end{aligned} \tag{3}$$

where $\mathcal{L}(\omega_\mathrm{p}) = 1/[(\omega_\mathrm{p} - \omega_0 - \delta\omega)^2 + \Gamma^2/4]$ is a Lorentzian profile with linewidth Γ, ω_p is the frequency of the probe field, and coefficient A and the phase ϕ depend on the mode matching of the probe and the collection mode. The resonance frequency shift $\delta\omega = \omega_z + \omega_\mathrm{ac}$ from the natural transition frequency ω_0 is due to a Zeeman shift ω_z and an ac Stark shift ω_ac. For perfect mode matching (e.g., when the collimation lens is identical to the focusing lens), the coefficients in Eq. (3) simplify to $A = \Gamma\Lambda$ and $\phi = 0$. The transmission spectrum takes a purely Lorentzian form with a resonant extinction $\epsilon = 4\Lambda(1 - \Lambda)$ [20].

We measure the transmission of a weak probe field for $t_\mathrm{p} =$ 20 ms containing on average 550 photons per pulse. Tuning the frequency of the probe field, we find a maximum extinction $\epsilon = 17.7(1)\%$ (Fig. 3). The observed transmission spectrum shows a small deviation from a Lorentzian profile. This deviation is caused by the imperfect mode overlap between probe and collection mode. We infer a mode overlap of approximately 70% from the probe power measured at detector D_f, corrected for losses of the optical elements. To account for the small deviation from the ideal case, we include the phase ϕ as a free fit parameter. The model in Eq. (3) fits the observed values with four free parameters ($\chi^2_\mathrm{red} = 1.01$): frequency shift $\delta\omega = 48.03(3)$ MHz, spatial overlap $\Lambda = 4.67(2)\,\%$, phase $\phi_0 = 0.13(1)$ rad, and linewidth $\Gamma/2\pi = 6.9(1)$ MHz (slightly

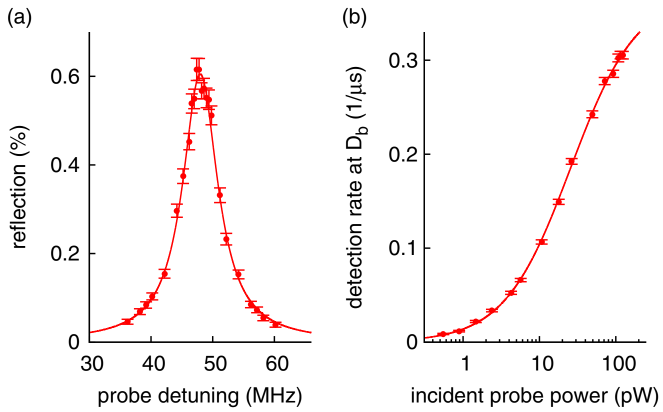

FIG. 4. (a) Light scattered into the backward detector D_b for different probe detunings. The solid line is a Lorentzian fit of Eq. (4) with free parameters linewidth $\Gamma/2\pi = 6.9(1)$ MHz, frequency shift $\delta\omega/2\pi = 48.0(1)$ MHz, and resonant backscattering probability $P_{b,0} = 0.61(1)\%$, with $\chi^2_{red} = 1.03$. (b) Resonant saturation measurement, with the solid line representing the fit of Eq. (6) with saturation power $P_{sat} = 26(2)$ pW and total detection efficiency $\eta = 1.95(2)\%$ as free parameters ($\chi^2_{red} = 1.3$). Error bars represent one standard deviation due to propagated Poissonian counting uncertainties.

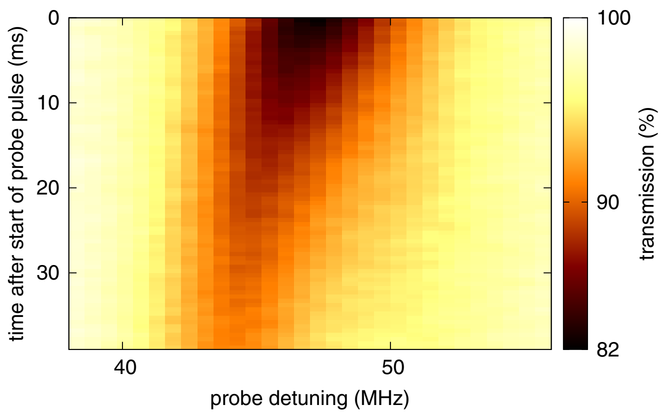

FIG. 5. Time-resolved extinction measurement. Each row presents a transmission spectrum similar to Fig. 3 and is obtained by collecting photodetection events in 0.5-ms-wide time bins. As the atom is heated by scattering probe photons, the transmission increases and the frequency of the minimal transmission shifts to a lower detuning from the unperturbed resonance.

broader than the natural linewidth $\Gamma_0/2\pi = 6.07$ MHz [34]). This interaction strength is 50% larger compared to our previous experiments with lenses of smaller numerical aperture (NA = 0.55 [18]).

IV. SATURATION MEASUREMENT

We also determine Λ from the intensity of the atomic fluorescence at backward detector D_b. Figure 4(a) shows the probability P_b for an incident photon to be backscattered by the atom when tuning the frequency ω_p of the probe field. This value is obtained by normalizing the number of detected photons at detector D_b to the average number of incident photons during the probe interval $t_p = 20\ \mu$s [35,36]. The backscattering probability is proportional to the atomic excited-state population and therefore follows a Lorentzian profile,

$$P_b = \frac{P_{b,0}}{4(\omega_p - \omega_0 - \delta\omega)^2/\Gamma^2 + 1}, \quad (4)$$

where $P_{b,0}$ is the *resonant* backscattering probability. The experimental values of P_b in Fig. 4 can be well described by this model, with a frequency shift $\delta\omega/2\pi = 48.0(1)$ MHz from the natural transition frequency, $P_{b,0} = 0.61(1)\%$, and $\Gamma/2\pi = 6.9(1)$ MHz.

The incident power needed to saturate the target transition is a direct measurement of Λ. For a resonantly driven two-level atom, the saturation power P_{sat} is given by

$$P_{sat} = \frac{\hbar\omega_0\Gamma_0}{8}\frac{1}{\Lambda}, \quad (5)$$

where ω_0 is the transition frequency [22]. For complete mode matching ($\Lambda = 1$), Eq. (5) gives a saturation power $P_{sat,\Lambda=1} = 1.21$ pW for the considered transition. The spatial overlap $\Lambda = P_{sat}/P_{sat,\Lambda=1}$ is obtained from the experimentally determined saturation power P_{sat}.

The saturation power P_{sat} is determined by varying the excitation power on resonance [see Fig. 4(b)]. We use a short probe interval ($t_p = 4\ \mu$s) to minimize heating of the atom. A saturation power of $P_{sat} = 26(2)$ pW and a total detection efficiency $\eta = 1.95(2)\%$ are obtained from fitting the resultant atomic fluorescence rate R_b to the expected saturation function,

$$R_b = \frac{\eta\Gamma_0}{2}\frac{P_{inc}}{P_{inc} + P_{sat}}, \quad (6)$$

where P_{inc} is the power of the incident beam at the position of the atom. We infer a total collection efficiency $\eta_{sm} = \eta/\eta_b = 3.3(3)\%$ into a single-mode fiber, which is compatible with the highest efficiencies reported for a free-space optic [37,38]. Comparing P_{sat} to $P_{sat,\Lambda=1}$ indicates a spatial overlap $\Lambda = 4.7(4)\%$, in agreement with the extinction measurement $\Lambda = 4.67(2)\ \%$. The uncertainty of the spatial overlap is dominated by the uncertainty of the efficiency η_f of detector D_f, which we use in conjunction with a set of calibrated neutral density filters to determine the incident power P_{inc}.

V. TEMPERATURE DEPENDENCE OF LIGHT-ATOM INTERACTION

We investigate whether the residual temperature of the atom limits the coupling to the probe field. As the recoil associated with the scattering of the probe field increases the kinetic energy of the atom, different atom temperatures can be accessed by following the temporal evolution of the probe transmission. The photodetection events during the probe interval are time tagged and sorted into 0.5-ms-wide time bins, resulting in the time-resolved transmission spectrum shown in Fig. 5. The probe pulse has a length of $t_p = 40$ ms and contains, on average, about 9000 photons. As the probe pulse progresses, the resonance frequency shifts towards lower frequencies and the extinction reduces.

Extracting the temperature dependency of the light-atom interaction directly from the time-resolved transmission spectrum (Fig. 5) is difficult because the scattering rate and

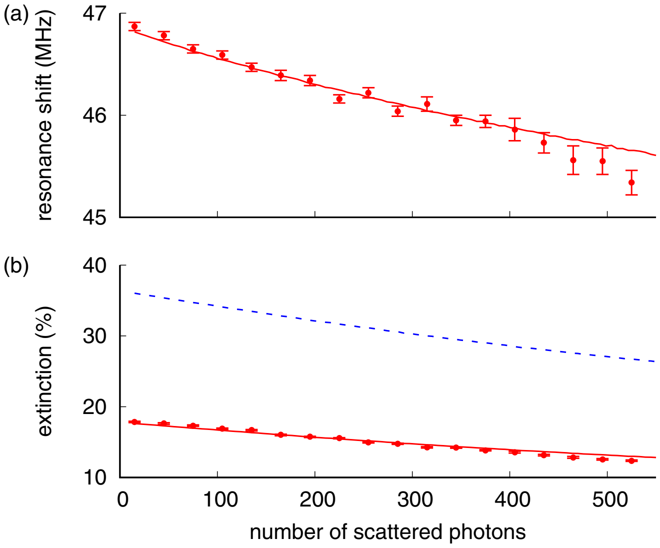

FIG. 6. The effect of recoil heating on the (a) resonance frequency and (b) extinction obtained by rearranging the histogram in Fig. 5 with a bin width of 30 scattered photons. Resonance frequency and extinction decrease fairly linearly as the atom heats up. (a) Solid red line is the numerical result of Eq. (8) with the frequency shift at the center of trap $\delta\omega(0)$ as a free fit parameter ($\chi^2_{\mathrm{red}} = 1.4$). (b) The temperature dependence is well reproduced by Eq. (8) with $\alpha = 0.54(1)$ as a free fit parameter (red solid line, $\chi^2_{\mathrm{red}} = 11.6$). The dashed blue line is the expected extinction for an ideal lens, given by Eq. (8), with $\alpha = 0$. Error bars represent one standard deviation obtained from the least-squares fit of the individual spectra.

therefore the motional heating vary during the probe interval and depend on the probe frequency. For a quantitative analysis, we sort the detection events for each probe frequency according to the number of scattered photons instead of the probe pulse duration t_{p}. The number of scattered photons, $n_{\mathrm{s}}(t)$, time integrated from the beginning of the probe interval to time t, is calculated from the transmitted photons via

$$n_{\mathrm{s}}(t) = \sum_{t_i=0}^{t} [n_{\mathrm{ref}}(t_i) - n_{\mathrm{p}}(t_i)]/\eta_{\mathrm{f}}\,\eta_{\mathrm{op}}, \tag{7}$$

where $n_{\mathrm{ref}}(t_i)$ and $n_{\mathrm{p}}(t_i)$ are the numbers of detected photons at detector D_{f} in time bin t_i during the reference and the probe interval, respectively, $\eta_{\mathrm{op}} = 59(5)\%$ is the optical loss from the atom to the detector, and η_{f} is the detection efficiency. We choose a relative bin width of 30 scattered photons and obtain the resonance frequency and the extinction by fitting to Eq. (3). The resonance frequency and the extinction decrease fairly linearly with the number of scattered photons (Fig. 6). After scattering approximately 500 photons, the resonance frequency is lowered by 1.5(1) MHz and the extinction is reduced by approximately 30 % to $\epsilon = 12.4(1)\%$.

We derive the temperature-dependent transmission spectrum by including the spatial dependence of the frequency shift $\delta\omega(\vec{r}) = \omega_z + \omega_{\mathrm{ac}}(\vec{r})$ and the mode overlap $\Lambda(\vec{r})$ [39] in Eq. (3), where $\vec{r}$ is the position of the atom relative to the center of the trap. The ac Stark shift $\omega_{\mathrm{ac}}(\vec{r})$ is treated in the paraxial approximation, given the large beam waist of 1.4 μm of the dipole trap. For the probe field, we use the effective interaction strength $\Lambda_{\mathrm{eff}}(\vec{r}) = (1-\alpha)\Lambda(\vec{r})$, where we evaluate the spatial dependence of the mode overlap $\Lambda(\vec{r})$ according to [13], which includes the changes of the local electric field polarization of the probe light near the focus. In addition, we heuristically introduce the parameter α which accounts for a reduced interaction strength due to experimental imperfections. The transmission spectrum, averaged over many different spatial configurations, is then given by

$$\langle\tau\rangle = \int p(T,\vec{r})\,\tau(\vec{r})d^3r, \tag{8}$$

where $p(T,\vec{r})$ is the probability distribution of the atom position. We treat the motion of the atom classically and assume that the probability distribution $p(T,\vec{r})$ is governed by a Maxwell-Boltzmann distribution with standard deviations of the positional spread of the atom $\sigma_i = \sqrt{k_{\mathrm{B}}T/mw_i^2}$, with $i = x,y,z$ and mass m of ^{87}Rb. Equation (8) can then be evaluated by a Monte Carlo method. Each scattered photon increases the total energy of the atom by $2E_{\mathrm{r}}$, where $E_{\mathrm{r}} = \hbar^2k^2/2m$ is the photon recoil energy. The gained energy is anisotropically distributed because of the unidirectional excitation by the probe beam. Each photon leads therefore, on average, to an energy increase of $\frac{2}{3}E_{\mathrm{r}}$ in the radial directions and $\frac{4}{3}E_{\mathrm{r}}$ in the axial direction. From a release-recapture technique [40], we infer an initial atom temperature of 21(1) μK. Thus, after 500 scattering events, the axial temperature is increased by approximately 120 μK to just below Doppler temperature, $T_{\mathrm{D}} = 146$ μK.

The frequency shift expected from Eq. (8) matches well with the experimental results [Fig. 6(a)], where we use only the frequency shift at the center of the trap $\delta\omega(0) = 47.32(5)$ MHz as a free fit parameter. This good agreement indicates that the model captures the effect of the dipole trap well. The initial resonance frequency is slightly lower compared to the results in Secs. IV and III because of a slightly lower dipole trap power. Figure 6(b) (solid red line) shows the theoretical extinction expected from Eq. (8) with our focusing parameters using $\alpha = 54(1)$ as a free parameter. The reduction of the extinction as a function of scattered photons is well reproduced by the model. From Eq. (8) with $\alpha = 0.54(1)$, we extrapolate a spatial overlap $\Lambda = 5.1\%$ for a stationary atom which is approximately 10% larger than the interaction observed for our lowest temperatures. This estimation provides an upper bound for the temperature effect because our model treats the atomic motion classically and therefore does not include the finite spread of the motional ground state. The large value of $\alpha = 0.54(1)$ means we observe less interaction compared to the tight focusing theory outlined in [13]. This reduction is likely to be caused by imperfections of the focusing lens and deviations of the incident field from a Gaussian beam.

Finally, we discuss possible origins of the observed linewidth broadening (Figs. 3 and 4). Doppler and power broadening are negligible because of the low atomic temperature of 21(1) μK and the weak excitation field in both measurements, $P_{\mathrm{probe}} < 0.02P_{\mathrm{sat}}$. We use Eq. (8) to estimate whether the broadening is caused by the thermal motion in the spatially varying trap potential. We find an expected linewidth of 6.3 MHz for $T = 21$ μK. Therefore, we attribute the residual linewidth broadening to other noise sources, such as the linewidth of the probe laser.

VI. CONCLUSION

We demonstrated an effective spatial mode overlap $\Lambda = 4.7(4)\%$ between an external probe mode and the atomic dipole mode, and showed that the light-atom interaction can be limited by the residual motion of the atom even at sub-Doppler temperatures. The spatially varying ac Stark shift and the tight confinement of the probe field cause a reduction of approximately 10% in interaction strength for our lowest atom temperatures. Thus, cooling to the motional ground state promises only a moderate improvement [41,42]. Further improvement of the interaction strength requires a more careful analysis of the focusing lens and the application of aberration corrections to the incident probe field. In addition, coherent control of the atomic motion and temporal shaping of the incoming photon can optimize the absorption efficiency [6,43].

ACKNOWLEDGMENTS

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