

# *Phase shift of a Weak Coherent Beam by a Single Atom*

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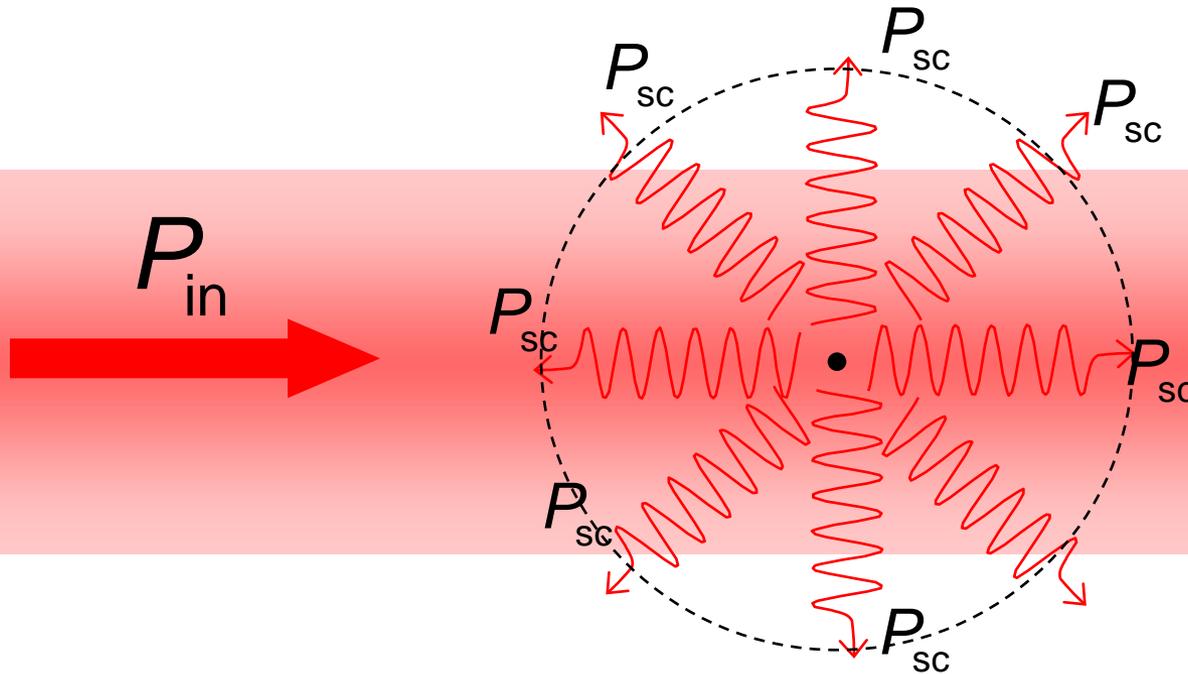


## ATOM-PHOTON INTERFACE

- Quantify interaction of a two-level atom with light
- Strong interaction without a cavity.
- Appropriate measurement

**Key idea for high efficiency:**

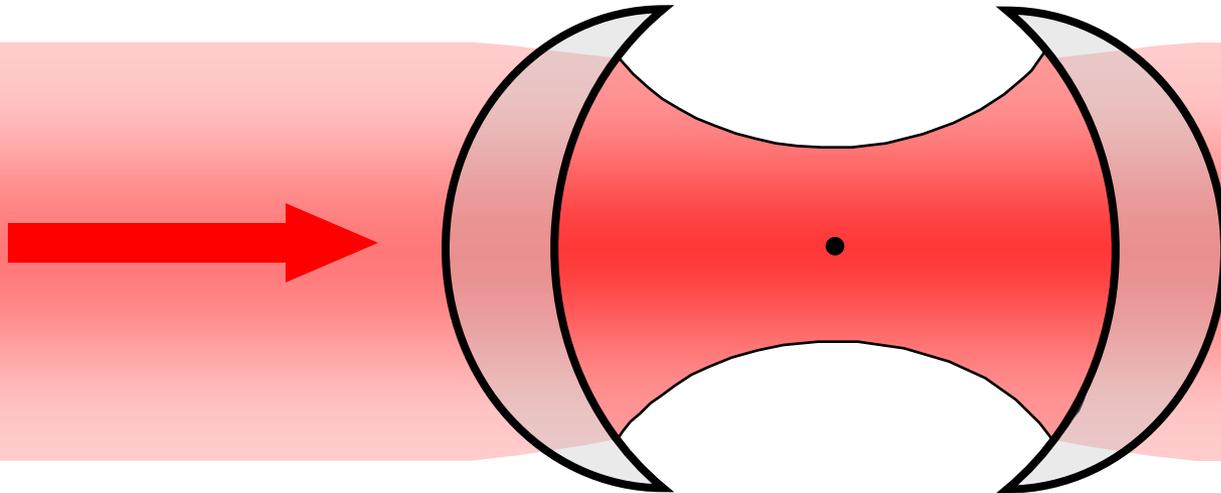
Try to **mode-match** flying qubit modes to field modes of spontaneous emission of a single atom



The scattering ratio  $R_{sc} = \frac{P_{sc}}{P_{in}}$

Concentration of the incoming field  
at the position of the atom is necessary!

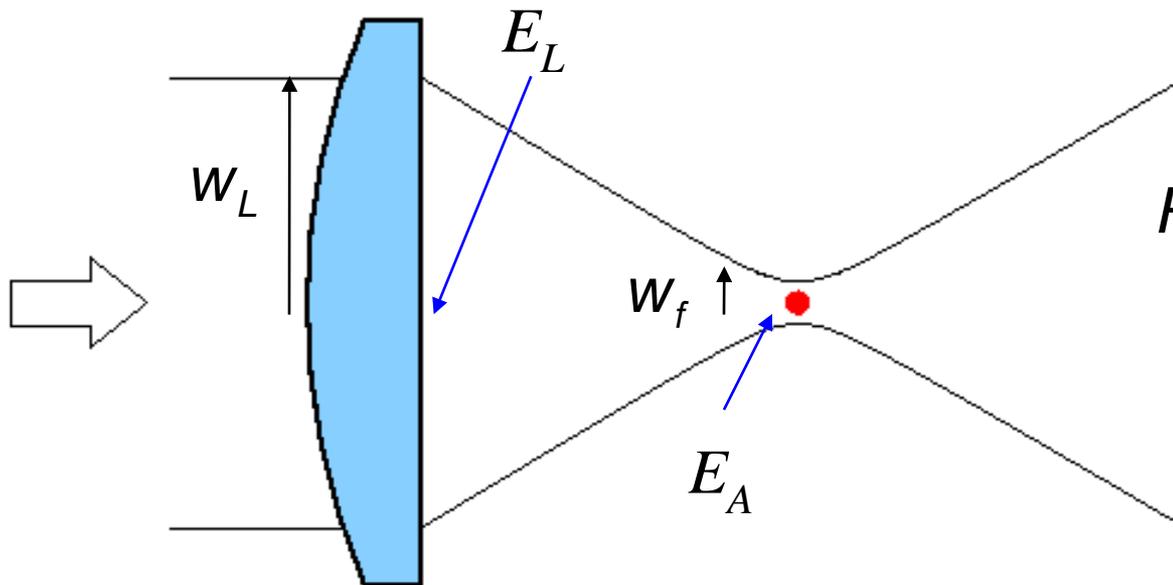
One solution: use a high-finesse cavity around the atom



Many ongoing experiments  
CalTech, Univ. of Georgia, Max-Planck-Institute, etc...

Or just use a (good) lens to focus light to an atom

Take a Gaussian beam (laser, single-mode fiber) and do estimation



paraxial approximation

$$R_{sc} = \frac{P_{sc}}{P_{in}} = \frac{3\lambda^2}{\pi W_L^2} \left( \frac{E_A}{E_L} \right)^2 \approx \frac{3\lambda^2}{\pi W_f^2} \approx \sigma_{\max} / A$$

Oversimplified model --- doesn't apply for strong focusing

- Let the field have a spherical wave front after the lens and write it in vectorial form compatible with Maxwell equations

- Propagate field to the focus

- mode decomposition

parabolic wavefront: S. van Enk et al., 2001,

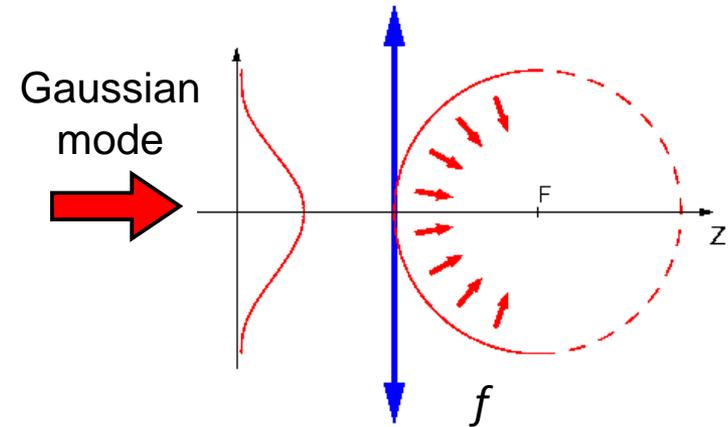
spherical wavefront: M.K. Tey et al., 2009.

- use Green theorem for a closed expression for field at focus  $E_A$

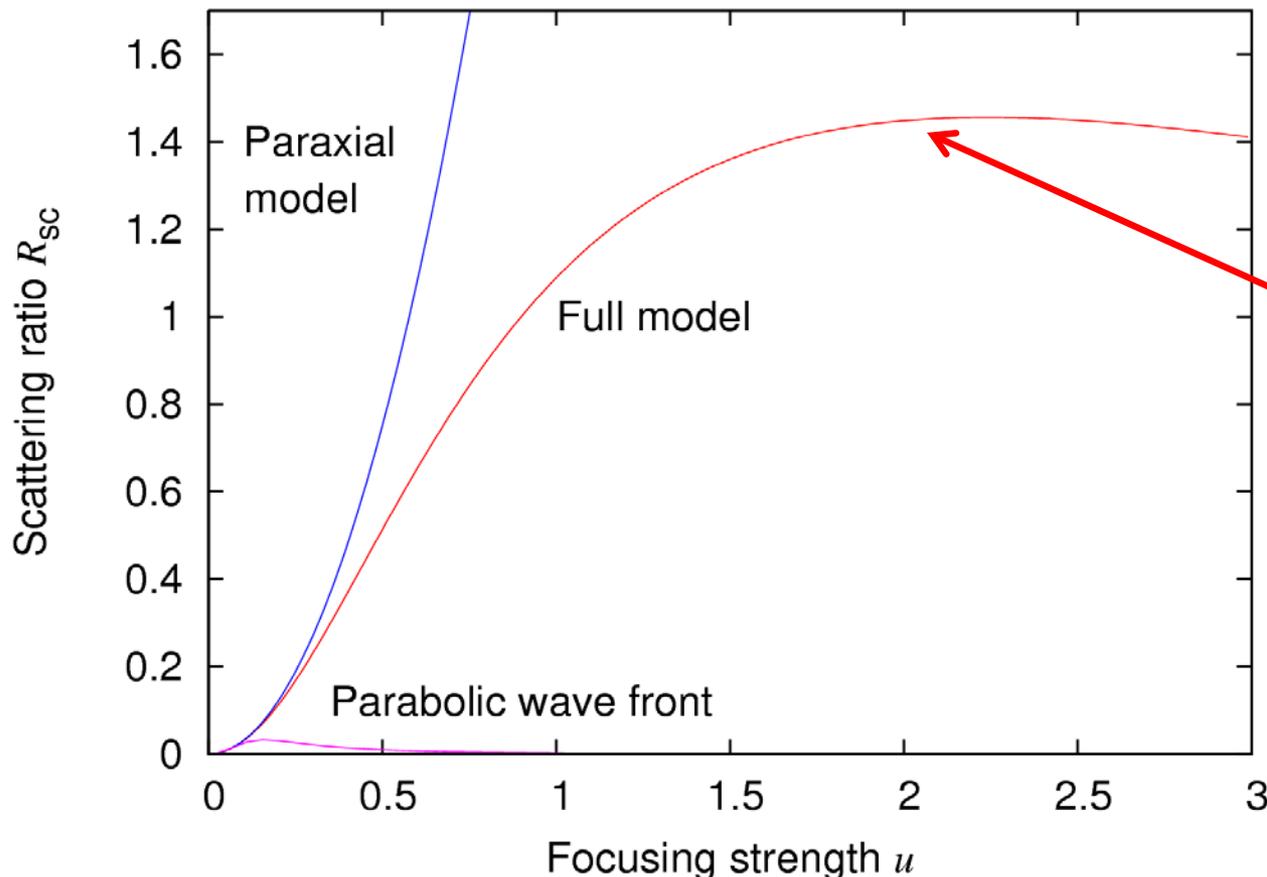
- determine atom response from semiclassical excitation probability for a given field

for weak, on-resonant excitation 
$$P_{sc} = \frac{3\epsilon_0 \lambda^2 E_A^2}{4\pi}$$

- obtain the scattering ratio 
$$R_{sc} = \frac{P_{sc}}{P_{in}}$$



Scattering ratio: 
$$R_{sc} := \frac{P_{sc}}{P_{in}} = \frac{3}{4u^3} e^{-2/u^2} \left[ \Gamma\left(-\frac{1}{4}, \frac{1}{u^2}\right) + u\Gamma\left(\frac{1}{4}, \frac{1}{u^2}\right) \right]^2$$



focusing strength

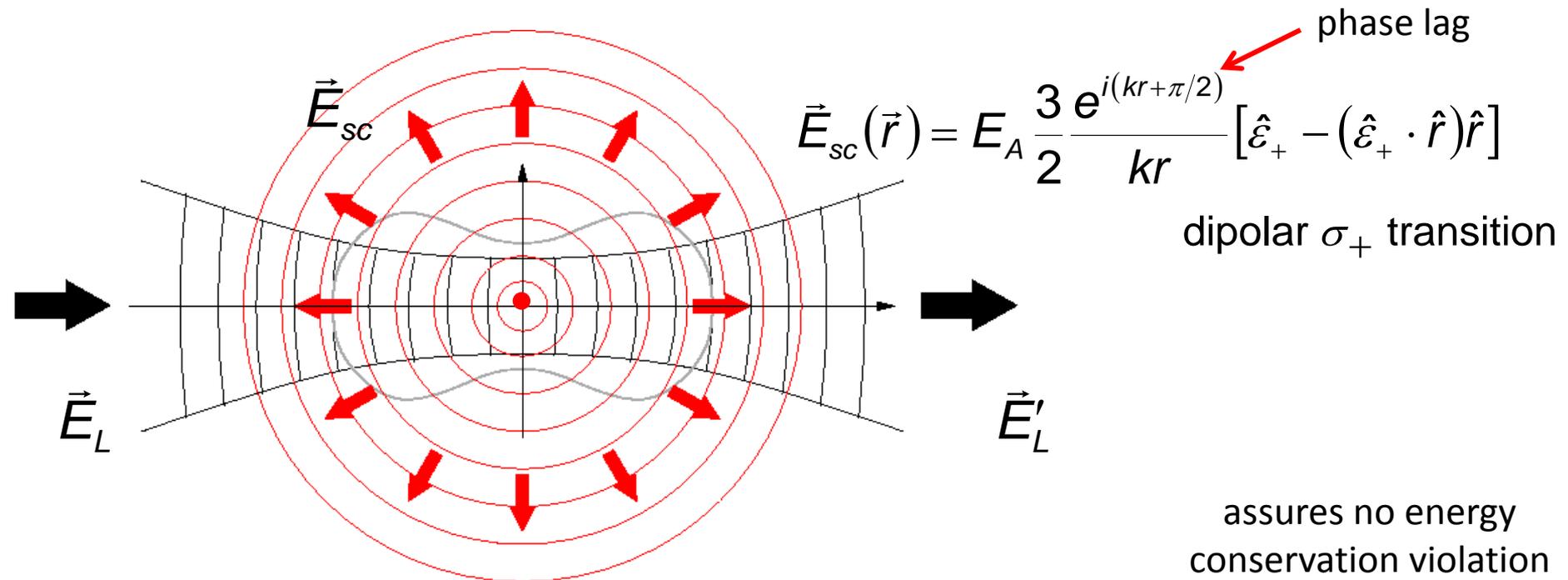
$$u = \frac{W_L}{f}$$

$R_{sc} > 1!!!$

Energy conserved!?!?

The total field is a superposition of the excitation and scattered field

$$\vec{E}_{Tot}(\vec{r}) = \vec{E}_{in}(\vec{r}) + \vec{E}_{sc}(\vec{r})$$



The outgoing power is defined up to a constant

$$P_{out} \equiv |\mathbf{E}_{Tot}|^2 = P_{in} + P_{sc} + \left( \vec{E}_{in}(\vec{r}) \cdot \vec{E}_{sc}^*(\vec{r}) \right) + \left( \vec{E}_{in}^*(\vec{r}) \cdot \vec{E}_{sc}(\vec{r}) \right)$$

Since no detector covers the full solid angle, we only partially collect the outgoing power

✓ natural choice --- projection onto the same mode as excitation

$$P_{out} = \left| \langle \vec{g}, \vec{E}_{Tot} \rangle \right|^2 \quad \langle \vec{g}, \vec{E} \rangle = \int_{\vec{x} \in S} \vec{E}_{Tot}(\vec{x}) \cdot \vec{g}(\vec{x}) (\vec{k}_g \cdot \vec{n}) dA$$

Integration can be carried out and we obtain experimentally measured quantities

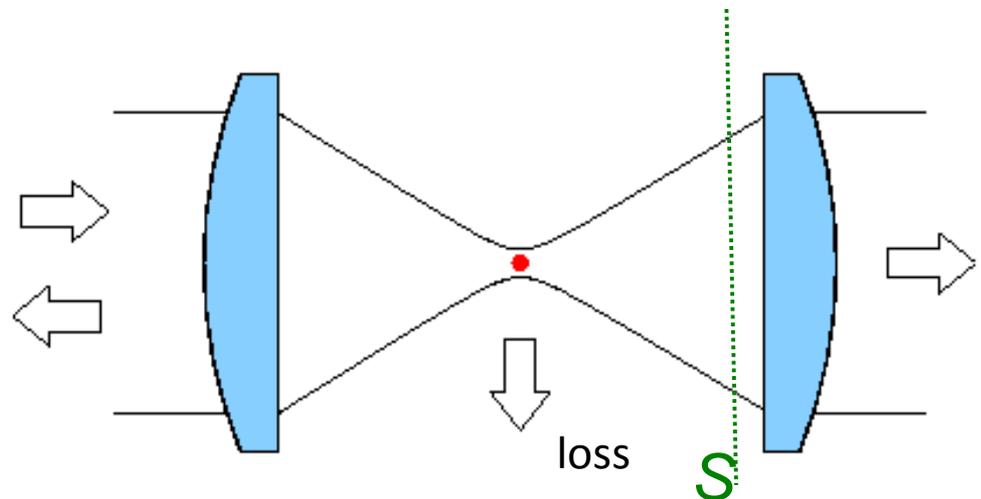
Forward transmission

$$T = 1 - \varepsilon = \frac{P_{out}}{P_{in}} = \left| 1 - \frac{R_{sc}}{2} \right|^2$$

Reflection

Losses

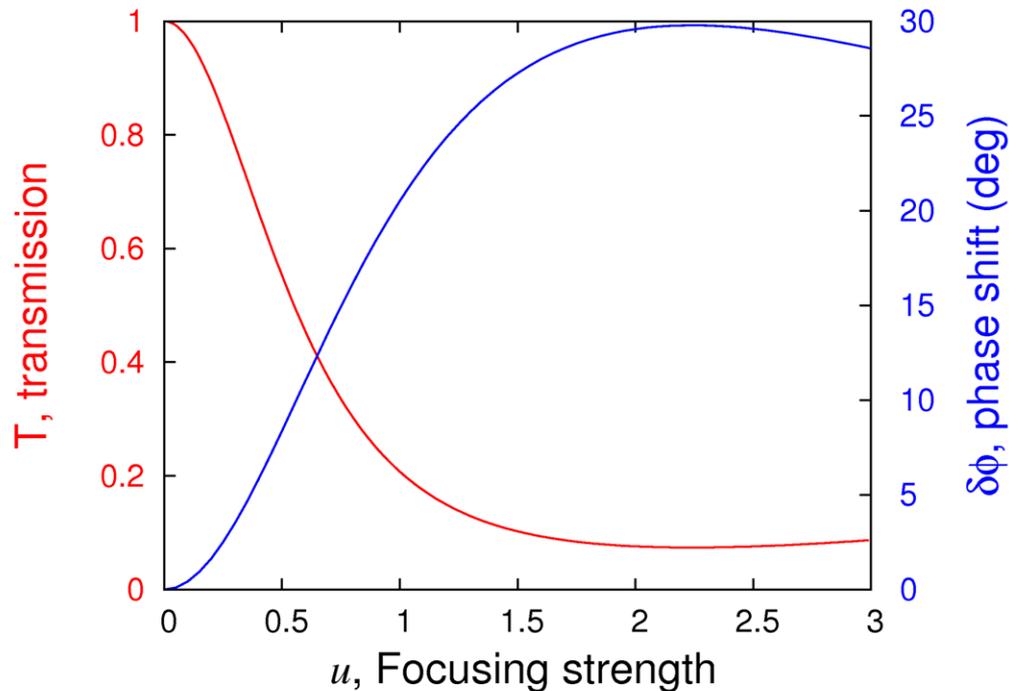
$$R = \frac{R_{sc}^2}{4} \quad L = R_{sc} - \frac{R_{sc}^2}{2}$$



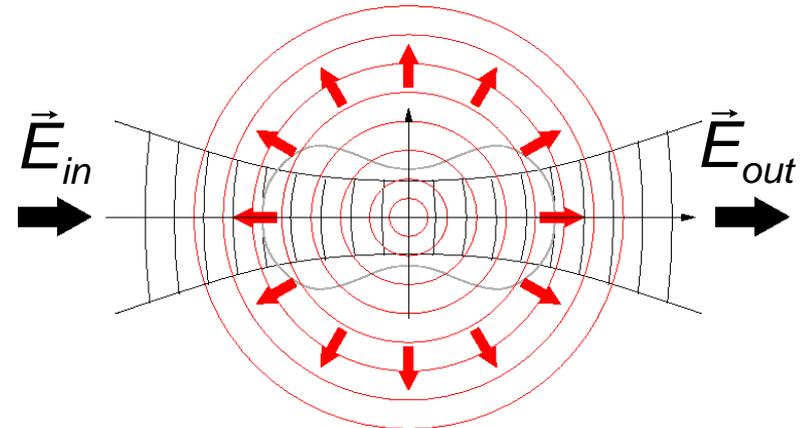
One also can estimate the phase shift that the atom imposes on a near-resonant light

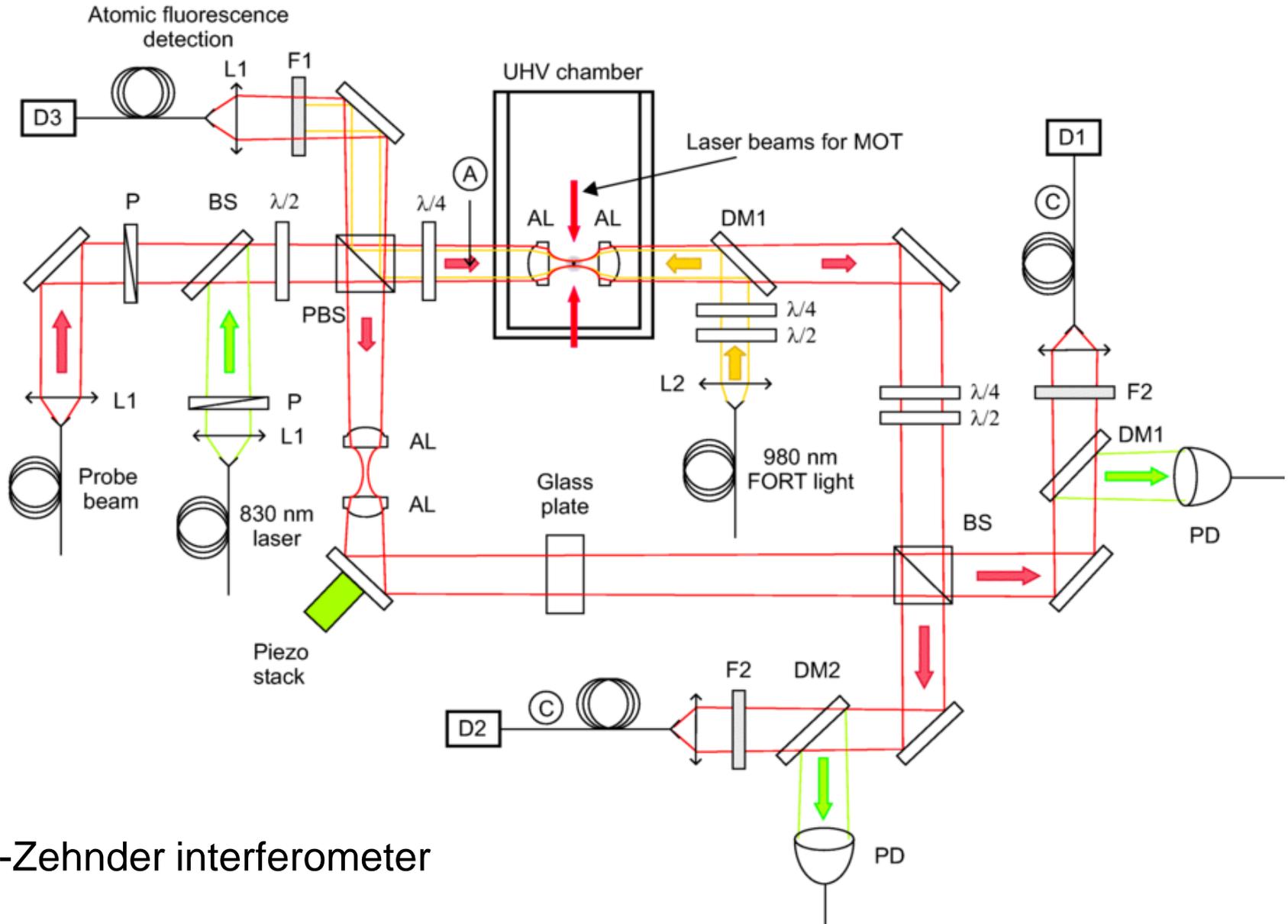
$$\delta\phi = \arg(\vec{E}_{out}(\vec{r}) \cdot \vec{E}_{in}^*(\vec{r})) = \arg\left(1 - \frac{R_{sc}}{2} \frac{i\Gamma}{2\Delta + i\Gamma}\right)$$

Lorentzian term

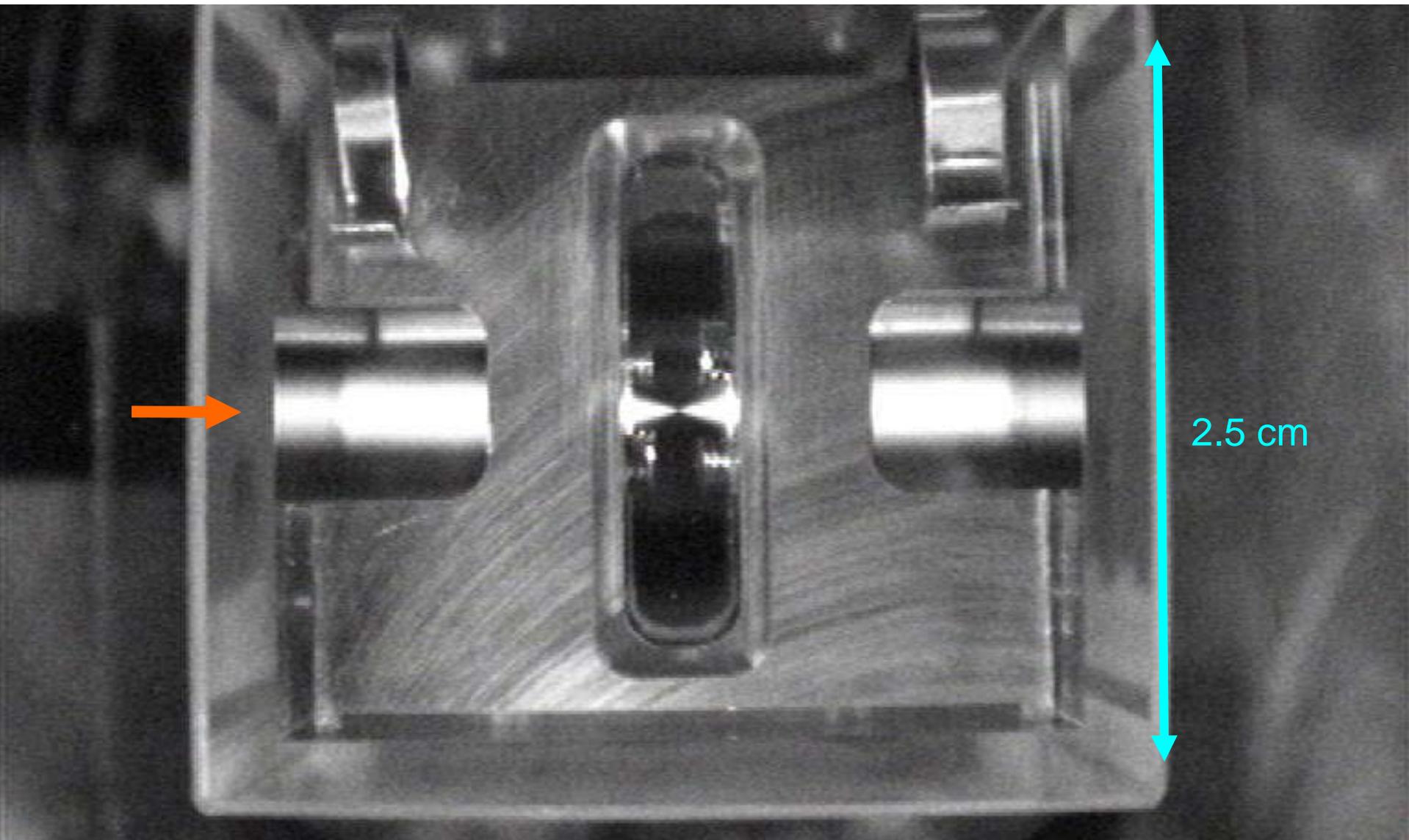


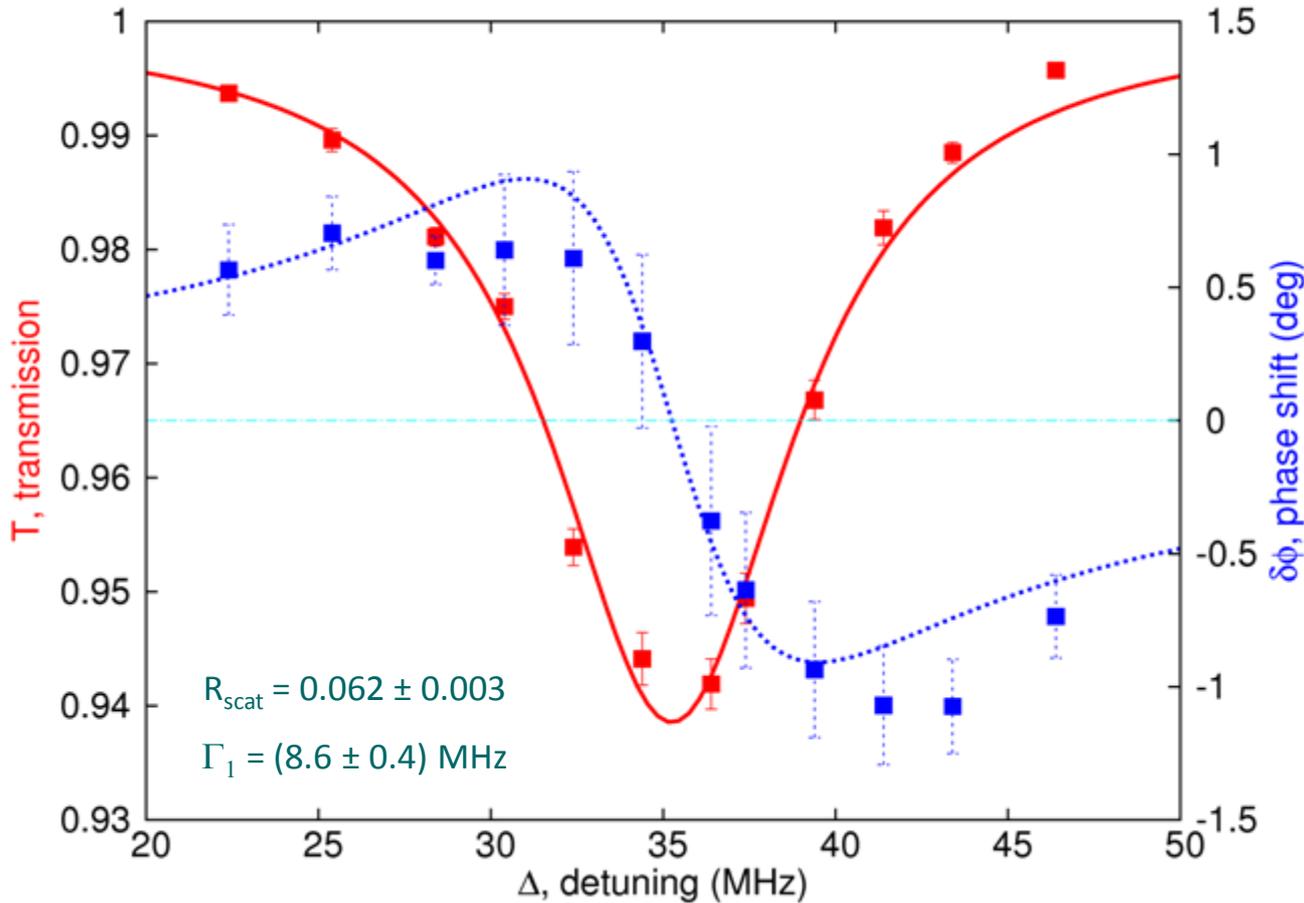
Gouy phase + "lag" of atomic response





Mach-Zehnder interferometer





Transmission of  
(95.9 ± 0.2)%

Max phase shift of  
(0.9 ± 0.2) ° at ~ $\Gamma/2$

Theoretical

Transmission: 84%

max phase shift: 2.3°

$$\delta\phi = \arg(\vec{E}_{\text{out}} \cdot \vec{E}_{\text{in}}^*) = \arg\left(4\Delta^2 + \Gamma^2\left(1 - \frac{R_{\text{scat}}}{2}\right) + iR_{\text{scat}}\Gamma\Delta\right)$$

$$T = \frac{|\vec{E}_{\text{out}}|^2}{|\vec{E}_{\text{in}}|^2} = \frac{4\Delta^2 + \Gamma^2\left(1 - \frac{R_{\text{scat}}}{2}\right)^2}{4\Delta^2 + \Gamma^2}$$

- Strong interaction of light with a single atom can be observed by simple focusing.
- $0.9^\circ$  phase shift of a weak coherent beam observed together with 95.9% transmission.

## Next steps

- Improve laser cooling
- Try larger numerical apertures
- Look for backscattered light
- Connect to nonclassical light sources....

## (almost) Hanbury-Brown—Twiss experiment on atomic fluorescence during cooling

